

# Optimal Dynamic Frequency Scaling for Energy - Performance of Parallel MPI Programs

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### **Outline**

- 1. Definitions and objectives
- 2. Energy and performance models
- 3. Performance and energy reduction trade-off
- 4. Experimental results and comparison
- 5. Conclusions and future works



### **Definitions**

- Modern processors provide Dynamic Voltage and Frequency Scaling (DVFS) technique.
- DVFS is used to reduce the frequency and thus to reduce the energy consumption by a CPU while computing.
- But scaling the frequency to lower level reduces the performance (execution time) of parallel program.
- Energy consumption for individual processor depends on two power metrics: the static power P<sub>static</sub> and the dynamic power P<sub>dyn</sub>.



### **Definitions**



- $P_{dyn} = \alpha \cdot C_L \cdot V^2 \cdot F$ .
- $P_{static} = V \cdot N_{trans} \cdot K_{design} \cdot I_{leak}$ .
- Energy consumption by individual processor of a synchronous parallel program:

$$E_{ind} = P_{dyn} \cdot T_{Comp} + P_{static} \cdot (T_{Comp} + T_{Comm}).$$

• The frequency scaling factor is the ratio between the maximum and the new frequency,  $S = \frac{F_{max}}{F_{new}}$ .



# **Objectives**

- Study the effect of the scaling factor S on energy consumption of parallel iterative applications such as NAS Benchmarks.
- Study the effect of the scaling factor S on performance of these benchmarks.
- Discovering the energy-performance trade-off relation when changing the frequency.
- We propose an algorithm for selecting the scaling factor S
  producing optimal trade-off between the energy and
  performance.
- Improving Rauber and Rünger's<sup>1</sup> method that our method best on.

Thomas Rauber and Gudula Rünger. Analytical modeling and simulation of the energy consumption of independent tasks. In Proceedings of the Winter Simulation Conference, 2012.



# **Energy model for homogeneous platform**



The dynamic power is **exponentially** related to the scaling factor *S* and the static consumed energy is **linearly** related to this factor.

### Rauber and Rünger's energy model

$$E = P_{\textit{dyn}} \cdot S_1^{-2} \cdot \left( T_1 + \sum_{i=2}^N rac{T_i^3}{T_1^2} \right) + P_{\textit{static}} \cdot S_1 \cdot T_1 \cdot N$$

 $S_1$ : is the max. scaling factor,  $T_i$ : is the time of the slower task,  $T_i$ : is the time of the other tasks and N: is the number of nodes.

### Rauber and Rünger's optimal scaling factor

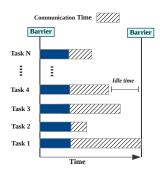
$$S_{opt} = \sqrt[3]{rac{2}{N} \cdot rac{P_{dyn}}{P_{static}} \cdot \left(1 + \sum_{i=2}^{N} rac{T_i^3}{T_1^3}
ight)}$$

They reduce degradation of the performance by setting the highest frequency to the slowest task.

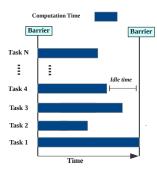


# Slack times of the sync. parallel program





(a) Sync. imbalanced communications



(b) Sync. imbalanced computations

**ProgramTime** =  $\max_{i=1,2,...,N} T_i$ 

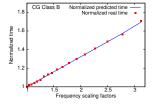


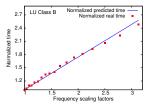
# Performance evaluation of MPI programs



#### **Execution time prediction model**

$$T_{new} = T_{MaxCompOld} \cdot S + T_{MaxCommOld}$$

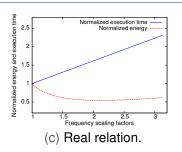


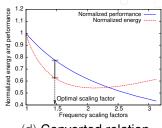


The maximum normalized error for CG=0.0073 (the smallest) and LU=0.031 (the worst).



# Performance and energy reduction trade-off





(d) Converted relation.

$$Performance = \frac{1}{execution \ time}$$

### Our objective function

$$\textit{MaxDist} = \max_{j=1,2,...,F} (\overbrace{P_{Norm}(S_j)}^{\textit{Maximize}} - \overbrace{E_{Norm}(S_j)}^{\textit{Minimize}})$$



# Scaling factor selection algorithm



Enumerate the available scaling factors and find  $S_{optimal}$  for which  $P_{Norm} - E_{Norm}$  is maximal.

### Where:

$$\overline{E_{Norm}} = \frac{E_{Reduced}}{E_{Original}} = \frac{P_{dyn} \cdot S_1^{-2} \cdot \left(T_1 + \sum_{i=2}^{N} \frac{T_i^3}{T_1^2}\right) + P_{static} \cdot T_1 \cdot S_1 \cdot N}{P_{dyn} \cdot \left(T_1 + \sum_{i=2}^{N} \frac{T_i^3}{T_1^2}\right) + P_{static} \cdot T_1 \cdot N}$$

$$P_{Norm} = rac{T_{old}}{T_{new}} = rac{T_{MaxCompOld} + T_{MaxCommOld}}{T_{MaxCompOld} \cdot S + T_{MaxCommOld}}$$



# Scaling factor selection algorithm



### **Algorithm characteristics**

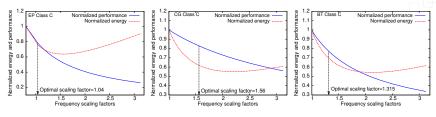
- It works online.
- It predicts both the energy consumption and performance.
- It is simultaneously reduces the energy consumption and maintaining performance of iterative algorithm.
- It takes into account the communication time.
- It is well adapted to imbalanced tasks.  $F_i = rac{F_{max} \cdot T_i}{S_{optimal} \cdot T_{max}}$
- It has a very small overhead. It takes **6.65**  $\mu s$  for 32 nodes.

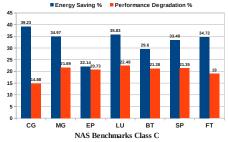
## **Experimental results**

- Our experiments are executed on the simulator SimGrid/SMPI v3.10.
- Our algorithm is applied to NAS parallel benchmarks.
- Each node in the cluster has 18 frequency values from 2.5 GHz to 800 MHz.
- We run the classes A, B and C on 4, 8 or 9 and 16 nodes respectively.
- The dynamic power with the highest frequency is equal to 20 W and the power static is equal to 4 W.



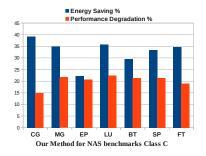
## **Experimental results**

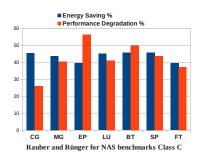






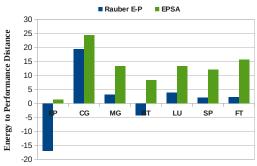
## **Results comparison**







## **Results comparison**



Comparing our method with Rauber and Rünger method for NAS benchmarks class C



### **Conclusions**

- We have presented a new online scaling factor selection method that optimizes simultaneously the energy and performance.
- It predicts the energy consumption and the performance of the parallel applications.
- Our algorithm saves more energy when the communication and the other slacks times are big.
- It gives the best trade-off between energy reduction and performance.
- Our method outperforms Rauber and Rünger's method in terms of energy-performance ratio.



### **Future works**

- We will apply the proposed algorithm to a heterogeneous platform.
- While the nodes of a heterogeneous platform are different in:
  - Dynamic and static power.
  - Individual energy consumption.
  - The available frequencies.
  - Performance capabilities.
- We will apply the proposed algorithm to a real cluster.
- We will apply the proposed algorithm to a real applications.



# **Thanks for Listening**



### To appear

This work will be appear in ISPA conference proceedings, August 2014

### Questions?

